Tables of sums of squares of Kronecker products

These tables give the sums of the squares of the Kronecker products of the irreducible representations of S_n described by partitions of n whose third part is 1 or 0. These are related to a problem posed by Luisa Carini (Palermo).

n = 2

$$2\{2\}$$

sum = 2

n = 3

$$3\{3\} \qquad + \{21\} \qquad + \{1^3\}$$

sum = 5

n = 4

$$5\{4\} \qquad + 2\{31\} \qquad + 3\{2^2\} \qquad + 2\{21^2\} \qquad + \{1^4\}$$

sum = 13

n = 5

$7\{5\}$	$+ 5\{41\}$	$+ 6\{32\}$	$+ 5\{31^2\}$	$+ 4\{2^21\}$
$+ 3\{21^3\}$	$+ \{1^5\}$			

sum = 31

n = 6

$10\{6\}$	$+ 8\{51\}$	$+ 14\{42\}$	$+ 10\{41^2\}$	$+ 4\{3^2\}$
$+ 13\{321\}$	$+ 9\{31^3\}$	$+ 7\{2^3\}$	$+ 5\{2^21^2\}$	$+ 4\{21^4\}$
$+ \{1^6\}$				

sum = 85

n = 7

$13\{7\}$	$+ 13\{61\}$	$+ 23\{52\}$	$+ 17\{51^2\}$	$+ 16\{43\}$
$+ 32\{421\}$	$+ 18\{41^3\}$	$+ 16\{3^21\}$	$+ 19\{32^2\}$	$+ 24\{321^2\}$
$+ 11\{31^4\}$	$+ 10\{2^31\}$	$+ 9\{2^21^3\}$	$+ 4\{21^5\}$	$+ \{1^7\}$

sum = 226

n = 8

$17\{8\}$	$+ 18\{71\}$	$+ 37\{62\}$	$+ 26\{61^2\}$	$+ 31\{53\}$
$+ 59\{521\}$	$+ 32\{51^3\}$	$+ 18\{4^2\}$	$+ 53\{431\}$	$+ 48\{42^2\}$
$+ 59\{421^2\}$	$+ 24\{41^4\}$	$+ 26\{3^22\}$	$+ 37\{3^21^2\}$	$+ 42\{32^21\}$
$+ 37\{321^3\}$	$+ 12\{31^5\}$	$+ 13\{2^4\}$	$+ 14\{2^31^2\}$	$+ 11\{2^21^4\}$
$+ 4\{21^6\}$	$+ \{1^8\}$			

sum = 619

n = 9

$21\{9\}$ $+ 25\{81\}$ $+ 52\{72\}$ $+ 37\{71^2\}$ $+ 55\{63\}$
$+ 96\{621\}$ $+ 49\{61^3\}$ $+ 41\{54\}$ $+ 112\{531\}$ $+ 89\{52^2\}$
$+ 115\{521^2\}$ $+ 43\{51^4\}$ $+ 55\{4^21\}$ $+ 96\{432\}$ $+ 116\{431^2\}$
$+ 113\{42^21\}$ $+ 93\{421^3\}$ $+ 28\{41^5\}$ $+ 22\{3^3\}$ $+ 80\{3^221\}$
$+ 55\{3^21^3\}$ $+ 45\{32^3\}$ $+ 71\{32^21^2\}$ $+ 45\{321^4\}$ $+ 13\{31^6\}$
$+ 19\{2^41\}$ $+ 21\{2^31^3\}$ $+ 11\{2^21^5\}$ $+ 4\{21^7\}$ $+ \{1^9\}$

sum = 1623

n = 10

$26\{10\ \}$ $+ 32\{91\}$ $+ 72\{82\}$ $+ 50\{81^2\}$ $+ 82\{73\}$
$+ 141\{721\}$ $+ 71\{71^3\}$ $+ 80\{64\}$ $+ 195\{631\}$ $+ 148\{62^2\}$
$+ 188\{621^2\}$ $+ 68\{61^4\}$ $+ 26\{5^2\}$ $+ 150\{541\}$ $+ 211\{532\}$
$+ 253\{531^2\}$ $+ 225\{52^21\}$ $+ 182\{521^3\}$ $+ 51\{51^5\}$ $+ 116\{4^22\}$
$+ 114\{4^21^2\}$ $+ 81\{43^2\}$ $+ 286\{4321\}$ $+ 186\{431^3\}$ $+ 123\{42^3\}$
$+ 193\{42^21^2\}$ $+ 120\{421^4\}$ $+ 30\{41^6\}$ $+ 75\{3^31\}$ $+ 82\{3^22^2\}$
$+ 148\{3^221^2\}$ $+ 68\{3^21^4\}$ $+ 94\{32^31\}$ $+ 99\{32^21^3\}$ $+ 50\{321^5\}$
$+ 13\{31^7\}$ $+ 19\{2^5\}$ $+ 26\{2^41^2\}$ $+ 24\{2^31^4\}$ $+ 11\{2^21^6\}$
$+ 4\{21^8\}$ $+ \{1^{10}\ \}$

sum = 4214

n = 11

$31\{11\ \}$ $+ 41\{10\ 1\}$ $+ 93\{92\}$ $+ 65\{91^2\}$ $+ 118\{83\}$
$+ 196\{821\}$ $+ 96\{81^3\}$ $+ 125\{74\}$ $+ 300\{731\}$ $+ 219\{72^2\}$
$+ 282\{721^2\}$ $+ 99\{71^4\}$ $+ 75\{65\}$ $+ 294\{641\}$ $+ 380\{632\}$
$+ 439\{631^2\}$ $+ 382\{62^21\}$ $+ 302\{621^3\}$ $+ 83\{61^5\}$ $+ 118\{5^21\}$
$+ 325\{542\}$ $+ 341\{541^2\}$ $+ 194\{53^2\}$ $+ 648\{5321\}$ $+ 411\{531^3\}$
$+ 244\{52^3\}$ $+ 398\{52^21^2\}$ $+ 238\{521^4\}$ $+ 57\{51^6\}$ $+ 129\{4^23\}$
$+ 337\{4^221\}$ $+ 197\{4^21^3\}$ $+ 290\{43^21\}$ $+ 320\{432^2\}$ $+ 533\{4321^2\}$
$+ 247\{431^4\}$ $+ 269\{42^31\}$ $+ 276\{42^21^3\}$ $+ 136\{421^5\}$ $+ 31\{41^7\}$
$+ 103\{3^32\}$ $+ 143\{3^31^2\}$ $+ 213\{3^22^21\}$ $+ 205\{3^221^3\}$ $+ 81\{3^21^5\}$
$+ 78\{32^4\}$ $+ 145\{32^31^2\}$ $+ 116\{32^21^4\}$ $+ 52\{321^6\}$ $+ 13\{31^8\}$
$+ 28\{2^51\}$ $+ 36\{2^41^3\}$ $+ 24\{2^31^5\}$ $+ 11\{2^21^7\}$ $+ 4\{21^9\}$
$+ \{1^{11}\ \}$

sum = 10612

n = 12

$37\{12\,\}$ $+ 50\{11\,1\}$ $+ 119\{10\,2\}$ $+ 82\{10\,1^2\}$ $+ 157\{93\}$
$+ 259\{921\}$ $+ 126\{91^3\}$ $+ 186\{84\}$ $+ 429\{831\}$ $+ 308\{82^2\}$
$+ 393\{821^2\}$ $+ 136\{81^4\}$ $+ 134\{75\}$ $+ 481\{741\}$ $+ 595\{732\}$
$+ 684\{731^2\}$ $+ 580\{72^21\}$ $+ 455\{721^3\}$ $+ 122\{71^5\}$ $+ 59\{6^2\}$
$+ 314\{651\}$ $+ 656\{642\}$ $+ 671\{641^2\}$ $+ 360\{63^2\}$ $+ 1172\{6321\}$
$+ 729\{631^3\}$ $+ 421\{62^3\}$ $+ 683\{62^21^2\}$ $+ 404\{621^4\}$ $+ 94\{61^6\}$
$+ 271\{5^22\}$ $+ 295\{5^21^2\}$ $+ 400\{543\}$ $+ 1017\{5421\}$ $+ 586\{541^3\}$
$+ 704\{53^21\}$ $+ 741\{532^2\}$ $+ 1231\{5321^2\}$ $+ 555\{531^4\}$ $+ 565\{52^31\}$
$+ 577\{52^21^3\}$ $+ 278\{521^5\}$ $+ 61\{51^7\}$ $+ 90\{4^3\}$ $+ 451\{4^231\}$
$+ 418\{4^22^2\}$ $+ 639\{4^221^2\}$ $+ 281\{4^21^4\}$ $+ 425\{43^22\}$ $+ 587\{43^21^2\}$
$+ 815\{432^21\}$ $+ 772\{4321^3\}$ $+ 295\{431^5\}$ $+ 228\{42^4\}$ $+ 422\{42^31^2\}$
$+ 337\{42^21^4\}$ $+ 144\{421^6\}$ $+ 32\{41^8\}$ $+ 68\{3^4\}$ $+ 276\{3^321\}$
$+ 209\{3^31^3\}$ $+ 170\{3^22^3\}$ $+ 352\{3^22^21^2\}$ $+ 248\{3^221^4\}$ $+ 88\{3^21^6\}$
$+ 154\{32^41\}$ $+ 189\{32^31^3\}$ $+ 125\{32^21^5\}$ $+ 52\{321^7\}$ $+ 13\{31^9\}$
$+ 25\{2^6\}$ $+ 38\{2^51^2\}$ $+ 40\{2^41^4\}$ $+ 24\{2^31^6\}$ $+ 11\{2^21^8\}$
$+ 4\{21^{10}\,\}$ $+ \{1^{12}\,\}$

sum = 26200

n = 13

$43\{13\,\}$ $+ 61\{12\,1\}$ $+ 146\{11\,2\}$ $+ 101\{11\,1^2\}$ $+ 205\{10\,3\}$
$+ 332\{10\,21\}$ $+ 159\{10\,1^3\}$ $+ 253\{94\}$ $+ 580\{931\}$ $+ 409\{92^2\}$
$+ 525\{921^2\}$ $+ 179\{91^4\}$ $+ 217\{85\}$ $+ 717\{841\}$ $+ 864\{832\}$
$+ 978\{831^2\}$ $+ 823\{82^21\}$ $+ 639\{821^3\}$ $+ 170\{81^5\}$ $+ 132\{76\}$
$+ 583\{751\}$ $+ 1090\{742\}$ $+ 1121\{741^2\}$ $+ 583\{73^2\}$ $+ 1858\{7321\}$
$+ 1144\{731^3\}$ $+ 642\{72^3\}$ $+ 1052\{72^21^2\}$ $+ 614\{721^4\}$ $+ 141\{71^6\}$
$+ 232\{6^21\}$ $+ 748\{652\}$ $+ 765\{651^2\}$ $+ 840\{643\}$ $+ 2074\{6421\}$
$+ 1171\{641^3\}$ $+ 1318\{63^21\}$ $+ 1377\{632^2\}$ $+ 2251\{6321^2\}$ $+ 1008\{631^4\}$
$+ 992\{62^31\}$ $+ 1004\{62^21^3\}$ $+ 481\{621^5\}$ $+ 102\{61^7\}$ $+ 390\{5^23\}$
$+ 917\{5^221\}$ $+ 510\{5^21^3\}$ $+ 290\{54^2\}$ $+ 1470\{5431\}$ $+ 1263\{542^2\}$
$+ 1987\{5421^2\}$ $+ 831\{541^4\}$ $+ 1062\{53^22\}$ $+ 1440\{53^21^2\}$ $+ 1933\{532^21\}$
$+ 1819\{5321^3\}$ $+ 680\{531^5\}$ $+ 478\{52^4\}$ $+ 914\{52^31^2\}$ $+ 717\{52^21^4\}$
$+ 305\{521^6\}$ $+ 63\{51^8\}$ $+ 304\{4^31\}$ $+ 727\{4^232\}$ $+ 944\{4^231^2\}$
$+ 1060\{4^22^21\}$ $+ 970\{4^221^3\}$ $+ 340\{4^21^5\}$ $+ 280\{43^3\}$ $+ 1184\{43^221\}$
$+ 889\{43^21^3\}$ $+ 692\{432^3\}$ $+ 1357\{432^21^2\}$ $+ 969\{4321^4\}$ $+ 324\{431^6\}$
$+ 467\{42^41\}$ $+ 565\{42^31^3\}$ $+ 371\{42^21^5\}$ $+ 149\{421^7\}$ $+ 32\{41^9\}$
$+ 189\{3^41\}$ $+ 252\{3^32^2\}$ $+ 474\{3^321^2\}$ $+ 265\{3^31^4\}$ $+ 392\{3^22^31\}$
$+ 458\{3^22^21^3\}$ $+ 280\{3^221^5\}$ $+ 89\{3^21^7\}$ $+ 111\{32^5\}$ $+ 227\{32^41^2\}$
$+ 215\{32^31^4\}$ $+ 128\{32^21^6\}$ $+ 52\{321^8\}$ $+ 13\{31^{10}\,\}$ $+ 37\{2^61\}$
$+ 51\{2^51^3\}$ $+ 40\{2^41^5\}$ $+ 24\{2^31^7\}$ $+ 11\{2^21^9\}$ $+ 4\{21^{11}\,\}$
$+ \{1^{13}\,\}$

sum = 62730

n = 14

$50\{14\ \}$ $+ 72\{13\ 1\}$ $+ 178\{12\ 2\}$ $+ 122\{12\ 1^2\}$ $+ 256\{11\ 3\}$

$+ 413\{11\ 21\}$ $+ 197\{11\ 1^3\}$ $+ 336\{10\ 4\}$ $+ 755\{10\ 31\}$ $+ 528\{10\ 2^2\}$

$+ 674\{10\ 21^2\}$ $+ 228\{10\ 1^4\}$ $+ 310\{95\}$ $+ 996\{941\}$ $+ 1179\{932\}$

$+ 1331\{931^2\}$ $+ 1107\{92^21\}$ $+ 856\{921^3\}$ $+ 225\{91^5\}$ $+ 240\{86\}$

$+ 933\{851\}$ $+ 1647\{842\}$ $+ 1675\{841^2\}$ $+ 859\{83^2\}$ $+ 2706\{8321\}$

$+ 1652\{831^3\}$ $+ 919\{82^3\}$ $+ 1501\{82^21^2\}$ $+ 872\{821^4\}$ $+ 198\{81^6\}$

$+ 78\{7^2\}$ $+ 571\{761\}$ $+ 1412\{752\}$ $+ 1442\{751^2\}$ $+ 1444\{743\}$

$+ 3510\{7421\}$ $+ 1965\{741^3\}$ $+ 2148\{73^21\}$ $+ 2209\{732^2\}$ $+ 3602\{7321^2\}$

$+ 1597\{731^4\}$ $+ 1546\{72^31\}$ $+ 1561\{72^21^3\}$ $+ 743\{721^5\}$ $+ 156\{71^7\}$

$+ 581\{6^22\}$ $+ 551\{6^21^2\}$ $+ 1104\{653\}$ $+ 2504\{6521\}$ $+ 1357\{651^3\}$

$+ 648\{64^2\}$ $+ 3116\{6431\}$ $+ 2634\{642^2\}$ $+ 4098\{6421^2\}$ $+ 1694\{641^4\}$

$+ 2037\{63^22\}$ $+ 2742\{63^21^2\}$ $+ 3618\{632^21\}$ $+ 3384\{6321^3\}$ $+ 1254\{631^5\}$

$+ 851\{62^4\}$ $+ 1626\{62^31^2\}$ $+ 1274\{62^21^4\}$ $+ 537\{621^6\}$ $+ 108\{61^8\}$

$+ 361\{5^24\}$ $+ 1510\{5^231\}$ $+ 1160\{5^22^2\}$ $+ 1851\{5^221^2\}$ $+ 723\{5^21^4\}$

$+ 1097\{54^21\}$ $+ 2405\{5432\}$ $+ 3112\{5431^2\}$ $+ 3350\{542^21\}$ $+ 3044\{5421^3\}$

$+ 1039\{541^5\}$ $+ 724\{53^3\}$ $+ 2993\{53^221\}$ $+ 2224\{53^21^3\}$ $+ 1672\{532^3\}$

$+ 3287\{532^21^2\}$ $+ 2330\{5321^4\}$ $+ 770\{531^6\}$ $+ 1025\{52^41\}$ $+ 1240\{52^31^3\}$

$+ 812\{52^21^5\}$ $+ 321\{521^7\}$ $+ 64\{51^9\}$ $+ 562\{4^32\}$ $+ 642\{4^31^2\}$

$+ 509\{4^23^2\}$ $+ 2054\{4^2321\}$ $+ 1494\{4^231^3\}$ $+ 959\{4^22^3\}$ $+ 1792\{4^22^21^2\}$

$+ 1258\{4^221^4\}$ $+ 378\{4^21^6\}$ $+ 862\{43^31\}$ $+ 1113\{43^22^2\}$ $+ 2079\{43^221^2\}$

$+ 1151\{43^21^4\}$ $+ 1578\{432^31\}$ $+ 1835\{432^21^3\}$ $+ 1108\{4321^5\}$ $+ 340\{431^7\}$

$+ 340\{42^5\}$ $+ 698\{42^41^2\}$ $+ 664\{42^31^4\}$ $+ 388\{42^21^6\}$ $+ 151\{421^8\}$

$+ 32\{41^{10}\ \}$ $+ 237\{3^42\}$ $+ 341\{3^41^2\}$ $+ 597\{3^32^21\}$ $+ 647\{3^321^3\}$

$+ 306\{3^31^5\}$ $+ 266\{3^22^4\}$ $+ 604\{3^22^31^2\}$ $+ 533\{3^22^21^4\}$ $+ 294\{3^221^6\}$

$+ 89\{3^21^8\}$ $+ 214\{32^51\}$ $+ 287\{32^41^3\}$ $+ 228\{32^31^5\}$ $+ 128\{32^21^7\}$

$+ 52\{321^9\}$ $+ 13\{31^{11}\ \}$ $+ 31\{2^7\}$ $+ 50\{2^61^2\}$ $+ 56\{2^51^4\}$

$+ 40\{2^41^6\}$ $+ 24\{2^31^8\}$ $+ 11\{2^21^{10}\ \}$ $+ 4\{21^{12}\ \}$ $+ \{1^{14}\ \}$

sum = 146871

n = 15

57{15 } + 85{14 1} + 211{13 2} + 145{13 1^2} + 316{12 3}
+ 504{12 21} + 238{12 1^3} + 425{11 4} + 952{11 31} + 659{11 2^2}
+ 844{11 21^2} + 283{11 1^4} + 427{10 5} + 1324{10 41} + 1548{10 32}
+ 1733{10 31^2} + 1436{10 $2^2$1} + 1104{10 21^3} + 289{10 1^5} + 363{96}
+ 1356{951} + 2307{942} + 2349{941^2} + 1192{93^2} + 3716{9321}
+ 2257{931^3} + 1240{92^3} + 2034{92^21^2} + 1174{921^4} + 265{91^6}
+ 202{87} + 1034{861} + 2292{852} + 2301{851^2} + 2220{843}
+ 5329{8421} + 2958{841^3} + 3178{$83^2$1} + 3257{832^2} + 5276{8321^2}
+ 2332{831^4} + 2231{$82^3$1} + 2244{82^21^3} + 1066{821^5} + 221{81^7}
+ 378{$7^2$1} + 1449{762} + 1414{761^2} + 2151{753} + 4791{7521}
+ 2571{751^3} + 1146{74^2} + 5424{7431} + 4497{742^2} + 7009{7421^2}
+ 2860{741^4} + 3365{$73^2$2} + 4498{73^21^2} + 5870{$732^2$1} + 5473{7321^3}
+ 2016{731^5} + 1334{72^4} + 2571{72^31^2} + 2005{72^21^4} + 845{721^6}
+ 167{71^8} + 907{$6^2$3} + 1930{$6^2$21} + 1007{6^21^3} + 1108{654}
+ 4270{6531} + 3277{652^2} + 5090{6521^2} + 1986{651^4} + 2488{$64^2$1}
+ 5204{6432} + 6677{6431^2} + 7061{$642^2$1} + 6370{6421^3} + 2155{641^5}
+ 1407{63^3} + 5815{$63^2$21} + 4309{63^21^3} + 3190{632^3} + 6225{632^21^2}
+ 4415{6321^4} + 1444{631^6} + 1858{$62^4$1} + 2243{62^31^3} + 1473{62^21^5}
+ 577{621^7} + 112{61^9} + 187{5^3} + 1498{$5^2$41} + 2546{$5^2$32}
+ 3253{5^231^2} + 3216{$5^22^2$1} + 2872{5^221^3} + 933{5^21^5} + 2037{$54^2$2}
+ 2405{54^21^2} + 1789{543^2} + 6926{54321} + 4972{5431^3} + 3043{542^3}
+ 5819{542^21^2} + 4007{5421^4} + 1200{541^6} + 2257{$53^3$1} + 2882{53^22^2}
+ 5337{53^221^2} + 2949{53^21^4} + 3892{$532^3$1} + 4531{532^21^3} + 2726{5321^5}
+ 824{531^7} + 742{52^5} + 1572{52^41^2} + 1484{52^31^4} + 873{52^21^6}
+ 329{521^8} + 65{51^{10} } + 520{$4^3$3} + 1591{$4^3$21} + 1063{4^31^3}
+ 1669{$4^23^2$1} + 2033{4^232^2} + 3678{4^2321^2} + 1983{4^231^4} + 2187{$4^22^3$1}
+ 2507{$4^22^21^3$} + 1459{4^221^5} + 408{4^21^7} + 1085{$43^3$2} + 1615{43^31^2}
+ 2692{$43^22^2$1} + 2901{43^221^3} + 1353{43^21^5} + 1127{432^4} + 2454{432^31^2}
+ 2202{432^21^4} + 1186{4321^6} + 347{431^8} + 673{$42^5$1} + 902{42^41^3}
+ 717{42^31^5} + 397{42^21^7} + 151{421^9} + 32{41^{11} } + 114{3^5}
+ 578{$3^4$21} + 499{3^41^3} + 440{3^32^3} + 946{$3^32^21^2$} + 775{3^321^4}
+ 328{3^31^6} + 579{$3^22^4$1} + 759{$3^22^31^3$} + 584{$3^22^21^5$} + 296{3^221^7}
+ 89{3^21^9} + 144{32^6} + 309{32^51^2} + 322{32^41^4} + 232{32^31^6}
+ 128{32^21^8} + 52{321^{10} } + 13{31^{12} } + 46{$2^7$1} + 66{2^61^3}
+ 56{2^51^5} + 40{2^41^7} + 24{2^31^9} + 11{2^21^{11} } + 4{21^{13} }
+ {1^{15} }

sum = 344939

n = 16

65{16 } $\quad$ + 98{15 1} $\quad$ + 249{14 2} $\quad$ + 170{14 1^2} $\quad$ + 379{13 3}
+ 603{13 21} $\quad$ + 284{13 1^3} $\quad$ + 530{12 4} $\quad$ + 1173{12 31} $\quad$ + 808{12 2^2}
+ 1031{12 21^2} $\quad$ + 344{12 1^4} $\quad$ + 554{11 5} $\quad$ + 1695{11 41} $\quad$ + 1963{11 32}
+ 2194{11 31^2} $\quad$ + 1806{11 2^{2}1} $\quad$ + 1385{11 21^3} $\quad$ + 360{11 1^5} $\quad$ + 521{10 6}
+ 1860{10 51} $\quad$ + 3090{10 42} $\quad$ + 3127{10 41^2} $\quad$ + 1578{10 3^2} $\quad$ + 4888{10 321}
+ 2955{10 31^3} $\quad$ + 1617{10 2^3} $\quad$ + 2647{10 2^{2}1^2} $\quad$ + 1524{10 21^4} $\quad$ + 342{10 1^6}
+ 347{97} $\quad$ + 1607{961} $\quad$ + 3360{952} $\quad$ + 3368{951^2} $\quad$ + 3160{943}
+ 7527{9421} $\quad$ + 4160{941^3} $\quad$ + 4424{93^{2}1} $\quad$ + 4501{932^2} $\quad$ + 7281{9321^2}
+ 3203{931^4} $\quad$ + 3043{92^{3}1} $\quad$ + 3057{92^{2}1^3} $\quad$ + 1448{921^5} $\quad$ + 299{91^7}
+ 138{8^2} $\quad$ + 927{871} $\quad$ + 2659{862} $\quad$ + 2559{861^2} $\quad$ + 3544{853}
+ 7784{8521} $\quad$ + 4139{851^3} $\quad$ + 1808{84^2} $\quad$ + 8376{8431} $\quad$ + 6899{842^2}
+ 10701{8421^2} $\quad$ + 4346{841^4} $\quad$ + 5034{83^{2}2} $\quad$ + 6706{83^{2}1^2} $\quad$ + 8695{832^{2}1}
+ 8086{8321^3} $\quad$ + 2970{831^5} $\quad$ + 1941{82^4} $\quad$ + 3737{82^{3}1^2} $\quad$ + 2914{82^{2}1^4}
+ 1225{821^6} $\quad$ + 240{81^8} $\quad$ + 982{7^{2}2} $\quad$ + 981{7^{2}1^2} $\quad$ + 2356{763}
+ 4959{7621} $\quad$ + 2577{761^3} $\quad$ + 2243{754} $\quad$ + 8397{7531} $\quad$ + 6336{752^2}
+ 9823{7521^2} $\quad$ + 3791{751^4} $\quad$ + 4495{74^{2}1} $\quad$ + 9157{7432} $\quad$ + 11707{7431^2}
+ 12222{742^{2}1} $\quad$ + 10990{7421^3} $\quad$ + 3692{741^5} $\quad$ + 2360{73^3} $\quad$ + 9674{73^{2}21}
+ 7141{73^{2}1^3} $\quad$ + 5234{732^3} $\quad$ + 10215{732^{2}1^2} $\quad$ + 7233{7321^4} $\quad$ + 2362{731^6}
+ 2968{72^{4}1} $\quad$ + 3584{72^{3}1^3} $\quad$ + 2356{72^{2}1^5} $\quad$ + 922{721^7} $\quad$ + 175{71^9}
+ 1042{6^{2}4} $\quad$ + 3505{6^{2}31} $\quad$ + 2634{6^{2}2^2} $\quad$ + 3964{6^{2}21^2} $\quad$ + 1527{6^{2}1^4}
+ 636{65^2} $\quad$ + 4554{6541} $\quad$ + 7388{6532} $\quad$ + 9331{6531^2} $\quad$ + 9083{652^{2}1}
+ 8038{6521^3} $\quad$ + 2595{651^5} $\quad$ + 4698{64^{2}2} $\quad$ + 5504{64^{2}1^2} $\quad$ + 3951{643^2}
+ 15154{64321} $\quad$ + 10827{6431^3} $\quad$ + 6515{642^3} $\quad$ + 12413{642^{2}1^2} $\quad$ + 8529{6421^4}
+ 2530{641^6} $\quad$ + 4484{63^{3}1} $\quad$ + 5686{63^{2}2^2} $\quad$ + 10510{63^{2}21^2} $\quad$ + 5801{63^{2}1^4}
+ 7500{632^{3}1} $\quad$ + 8735{632^{2}1^3} $\quad$ + 5260{6321^5} $\quad$ + 1579{631^7} $\quad$ + 1360{62^5}
+ 2890{62^{4}1^2} $\quad$ + 2740{62^{3}1^4} $\quad$ + 1613{62^{2}1^6} $\quad$ + 604{621^8} $\quad$ + 114{61^{10} }
+ 815{5^{3}1} $\quad$ + 2841{5^{2}42} $\quad$ + 3383{5^{2}41^2} $\quad$ + 2050{5^{2}3^2} $\quad$ + 7493{5^{2}321}
+ 5261{5^{2}31^3} $\quad$ + 2961{5^{2}2^3} $\quad$ + 5740{5^{2}2^{2}1^2} $\quad$ + 3843{5^{2}21^4} $\quad$ + 1117{5^{2}1^6}
+ 2000{54^{2}3} $\quad$ + 6022{54^{2}21} $\quad$ + 3979{54^{2}1^3} $\quad$ + 5842{543^{2}1} $\quad$ + 6966{5432^2}
+ 12607{54321^2} $\quad$ + 6737{5431^4} $\quad$ + 7181{542^{3}1} $\quad$ + 8239{542^{2}1^3} $\quad$ + 4773{5421^5}
+ 1314{541^7} $\quad$ + 2900{53^{3}2} $\quad$ + 4291{53^{3}1^2} $\quad$ + 7056{53^{2}2^{2}1} $\quad$ + 7600{53^{2}21^3}
+ 3539{53^{2}1^5} $\quad$ + 2820{532^4} $\quad$ + 6168{532^{3}1^2} $\quad$ + 5542{532^{2}1^4} $\quad$ + 2989{5321^6}
+ 853{531^8} $\quad$ + 1527{52^{5}1} $\quad$ + 2057{52^{4}1^3} $\quad$ + 1645{52^{3}1^5} $\quad$ + 907{52^{2}1^7}
+ 334{521^9} $\quad$ + 65{51^{11} } $\quad$ + 258{4^4} $\quad$ + 1711{4^{3}31} $\quad$ + 1699{4^{3}2^2}
+ 2906{4^{3}21^2} $\quad$ + 1453{4^{3}1^4} $\quad$ + 2165{4^{2}3^{2}2} $\quad$ + 3231{4^{2}3^{2}1^2} $\quad$ + 4959{4^{2}32^{2}1}
+ 5261{4^{2}321^3} $\quad$ + 2361{4^{2}31^5} $\quad$ + 1637{4^{2}2^4} $\quad$ + 3448{4^{2}2^{3}1^2} $\quad$ + 3085{4^{2}2^{2}1^4}
+ 1589{4^{2}21^6} $\quad$ + 424{4^{2}1^8} $\quad$ + 551{43^4} $\quad$ + 2774{43^{3}21} $\quad$ + 2372{43^{3}1^3}
+ 2026{43^{2}2^3} $\quad$ + 4342{43^{2}2^{2}1^2} $\quad$ + 3557{43^{2}21^4} $\quad$ + 1480{43^{2}1^6} $\quad$ + 2419{432^{4}1}
+ 3184{432^{3}1^3} $\quad$ + 2443{432^{2}1^5} $\quad$ + 1224{4321^7} $\quad$ + 348{431^9} $\quad$ + 452{42^6}
+ 982{42^{5}1^2} $\quad$ + 1039{42^{4}1^4} $\quad$ + 743{42^{3}1^6} $\quad$ + 400{42^{2}1^8} $\quad$ + 151{421^{10} }
+ 32{41^{12} } $\quad$ + 318{3^{5}1} $\quad$ + 494{3^{4}2^2} $\quad$ + 954{3^{4}21^2} $\quad$ + 623{3^{4}1^4}
+ 966{3^{3}2^{3}1} $\quad$ + 1229{3^{3}2^{2}1^3} $\quad$ + 860{3^{3}21^5} $\quad$ + 335{3^{3}1^7} $\quad$ + 362{3^{2}2^5}
+ 864{3^{2}2^{4}1^2} $\quad$ + 866{3^{2}2^{3}1^4} $\quad$ + 605{3^{2}2^{2}1^6} $\quad$ + 296{3^{2}21^8} $\quad$ + 89{3^{2}1^{10} }
+ 274{32^{6}1} $\quad$ + 385{32^{5}1^3} $\quad$ + 339{32^{4}1^5} $\quad$ + 232{32^{3}1^7} $\quad$ + 128{32^{2}1^9}
+ 52{321^{11} } $\quad$ + 13{31^{13} } $\quad$ + 37{2^8} $\quad$ + 62{2^{7}1^2} $\quad$ + 72{2^{6}1^4}
+ 56{2^{5}1^6} $\quad$ + 40{2^{4}1^8} $\quad$ + 24{2^{3}1^{10} } $\quad$ + 11{2^{2}1^{12} } $\quad$ + 4{21^{14} }
+ {1^{16} }

sum = 747037

n = 17

$73\{17\ \} + 113\{16\ 1\} + 288\{15\ 2\} + 197\{15\ 1^2\} + 451\{14\ 3\}$

$+ 712\{14\ 21\} + 333\{14\ 1^3\} + 641\{13\ 4\} + 1416\{13\ 31\} + 969\{13\ 2^2\}$

$+ 1239\{13\ 21^2\} + 411\{13\ 1^4\} + 705\{12\ 5\} + 2115\{12\ 41\} + 2432\{12\ 32\}$

$+ 2704\{12\ 31^2\} + 2221\{12\ 2^21\} + 1697\{12\ 21^3\} + 440\{12\ 1^5\} + 694\{11\ 6\}$

$+ 2437\{11\ 51\} + 3976\{11\ 42\} + 4025\{11\ 41^2\} + 2021\{11\ 3^2\} + 6222\{11\ 321\}$

$+ 3750\{11\ 31^3\} + 2038\{11\ 2^3\} + 3344\{11\ 2^21^2\} + 1918\{11\ 21^4\} + 429\{11\ 1^6\}$

$+ 539\{10\ 7\} + 2304\{10\ 61\} + 4644\{10\ 52\} + 4617\{10\ 51^2\} + 4272\{10\ 43\}$

$+ 10108\{10\ 421\} + 5561\{10\ 41^3\} + 5870\{10\ 3^21\} + 5961\{10\ 32^2\} + 9609\{10\ 321^2\}$

$+ 4220\{10\ 31^4\} + 3986\{10\ 2^31\} + 3996\{10\ 2^21^3\} + 1891\{10\ 21^5\} + 388\{10\ 1^7\}$

$+ 303\{98\} + 1632\{971\} + 4166\{962\} + 4023\{961^2\} + 5273\{953\}$

$+ 11483\{9521\} + 6077\{951^3\} + 2610\{94^2\} + 11990\{9431\} + 9794\{942^2\}$

$+ 15194\{9421^2\} + 6136\{941^4\} + 7056\{93^22\} + 9368\{93\ 21^2\} + 12087\{932^21\}$

$+ 11223\{9321^3\} + 4112\{931^5\} + 2658\{92^4\} + 5136\{92^31^2\} + 3997\{92^21^4\}$

$+ 1681\{921^6\} + 327\{91^8\} + 603\{8^21\} + 2448\{872\} + 2362\{871^2\}$

$+ 4394\{863\} + 9121\{8621\} + 4698\{861^3\} + 3804\{854\} + 13868\{8531\}$

$+ 10417\{852^2\} + 16035\{8521^2\} + 6170\{851^4\} + 7134\{84^21\} + 14275\{8432\}$

$+ 18185\{8431^2\} + 18855\{842^21\} + 16906\{8421^3\} + 5663\{841^5\} + 3555\{83^3\}$

$+ 14566\{83^221\} + 10740\{83\ 21^3\} + 7829\{832^3\} + 15234\{832^21^2\} + 10793\{8321^4\}$

$+ 3515\{831^6\} + 4359\{82^41\} + 5259\{82^31^3\} + 3465\{82^21^5\} + 1354\{821^7\}$

$+ 255\{81^9\} + 1690\{7^23\} + 3478\{7^221\} + 1789\{7^21^3\} + 2795\{764\}$

$+ 9284\{7631\} + 6781\{762^2\} + 10301\{7621^2\} + 3894\{761^4\} + 1390\{75^2\}$

$+ 9318\{7541\} + 14694\{7532\} + 18473\{7531^2\} + 17752\{752^21\} + 15650\{7521^3\}$

$+ 5018\{751^5\} + 8563\{74^22\} + 10054\{74^21^2\} + 7086\{743^2\} + 26896\{74321\}$

$+ 19144\{7431^3\} + 11377\{742^3\} + 21739\{742^21^2\} + 14886\{7421^4\} + 4412\{741^6\}$

$+ 7574\{73^31\} + 9573\{73^22^2\} + 17651\{73^221^2\} + 9745\{73^21^4\} + 12448\{732^31\}$

$+ 14508\{732^21^3\} + 8748\{7321^5\} + 2623\{731^7\} + 2183\{72^5\} + 4681\{72^41^2\}$

$+ 4437\{72^31^4\} + 2626\{72^21^6\} + 978\{721^8\} + 181\{71^{10}\ \} + 810\{6^25\}$

$+ 4252\{6^241\} + 6274\{6^232\} + 7779\{6^231^2\} + 7323\{6^22^21\} + 6388\{6^221^3\}$

$+ 2025\{6^21^5\} + 2778\{65^21\} + 8847\{6542\} + 10343\{6541^2\} + 6019\{653^2\}$

$+ 21957\{65321\} + 15355\{6531^3\} + 8541\{652^3\} + 16330\{652^21^2\} + 10953\{6521^4\}$

$+ 3132\{651^6\} + 4725\{64^23\} + 14038\{64^221\} + 9215\{64^21^3\} + 13067\{643^21\}$

$+ 15461\{6432^2\} + 27928\{64321^2\} + 14896\{6431^4\} + 15560\{642^31\} + 17850\{642^21^3\}$

$+ 10345\{6421^5\} + 2826\{641^7\} + 5823\{63^32\} + 8662\{63^31^2\} + 14088\{63^22^21\}$

$+ 15201\{63^221^3\} + 7080\{63^21^5\} + 5526\{632^4\} + 12048\{632^31^2\} + 10889\{632^21^4\}$

$+ 5878\{6321^6\} + 1669\{631^8\} + 2844\{62^51\} + 3842\{62^41^3\} + 3096\{62^31^5\}$

$+ 1708\{62^21^7\} + 620\{621^9\} + 115\{61^{11}\ \} + 1628\{5^32\} + 1874\{5^31^2\}$

$+ 3016\{5^243\} + 8693\{5^2421\} + 5621\{5^241^3\} + 6720\{5^23^21\} + 7703\{5^232^2\}$

$+ 13880\{5^2321^2\} + 7265\{5^231^4\} + 7217\{5^22^31\} + 8239\{5^22^21^3\} + 4693\{5^221^5\}$

$+ 1242\{5^21^7\} + 994\{54^3\} + 6729\{54^231\} + 6447\{54^22^2\} + 11220\{54^221^2\}$

$+ 5505\{54^21^4\} + 7745\{543^22\} + 11394\{543^21^2\} + 17296\{5432^21\} + 18334\{54321^3\}$

$+ 8211\{5431^5\} + 5383\{542^4\} + 11575\{542^31^2\} + 10292\{542^21^4\} + 5327\{5421^6\}$

$+ 1381\{541^8\} + 1494\{53^4\} + 7518\{53^321\} + 6424\{53^31^3\} + 5408\{53^22^3\}$

$+ 11550\{53^22^21^2\} + 9511\{53^221^4\} + 3948\{53^21^6\} + 6157\{532^41\} + 8149\{532^31^3\}$

$+ 6282\{532^21^5\} + 3140\{5321^7\} + 869\{531^9\} + 1013\{52^6\} + 2277\{52^51^2\}$

$+ 2410\{52^41^4\} + 1744\{52^31^6\} + 924\{52^21^8\} + 336\{521^{10}\ \} + 65\{51^{12}\ \}$

$+ 834\{4^41\} + 2375\{4^332\} + 3381\{4^331^2\} + 4168\{4^32^21\} + 4267\{4^321^3\}$

$+ 1747\{4^31^5\} + 1159\{4^23^3\} + 5718\{4^23^221\} + 4802\{4^23^21^3\} + 3864\{4^232^3\}$

$+ 8115\{4^232^21^2\} + 6581\{4^2321^4\} + 2623\{4^231^6\} + 3502\{4^22^41\} + 4592\{4^22^31^3\}$

$+ 3466\{4^22^21^5\} + 1671\{4^221^7\} + 427\{4^21^9\} + 1586\{43^41\} + 2363\{43^32^2\}$

$+ 4677\{43^321^2\} + 3003\{43^31^4\} + 4518\{43^22^31\} + 5753\{43^22^21^3\} + 4021\{43^221^5\}$

n = 17 (contd)

$+ 1543\{43^2 1^7\}$ $+ 1570\{432^5\}$ $+ 3631\{432^4 1^2\}$ $+ 3723\{432^3 1^4\}$ $+ 2572\{432^2 1^6\}$
$+ 1238\{4321^8\}$ $+ 348\{431^{10}\}$ $+ 879\{42^6 1\}$ $+ 1247\{42^5 1^3\}$ $+ 1111\{42^4 1^5\}$
$+ 756\{42^3 1^7\}$ $+ 400\{42^2 1^9\}$ $+ 151\{421^{11}\}$ $+ 32\{41^{13}\}$ $+ 360\{3^5 2\}$
$+ 569\{3^5 1^2\}$ $+ 1101\{3^4 2^2 1\}$ $+ 1298\{3^4 21^3\}$ $+ 701\{3^4 1^5\}$ $+ 636\{3^3 2^4\}$
$+ 1466\{3^3 2^3 1^2\}$ $+ 1429\{3^3 2^2 1^4\}$ $+ 904\{3^3 21^6\}$ $+ 336\{3^3 1^8\}$ $+ 766\{3^2 2^5 1\}$
$+ 1068\{3^2 2^4 1^3\}$ $+ 936\{3^2 2^3 1^5\}$ $+ 608\{3^2 2^2 1^7\}$ $+ 296\{3^2 21^9\}$ $+ 89\{3^2 1^{11}\}$
$+ 177\{32^7\}$ $+ 391\{32^6 1^2\}$ $+ 429\{32^5 1^4\}$ $+ 344\{32^4 1^6\}$ $+ 232\{32^3 1^8\}$
$+ 128\{32^2 1^{10}\}$ $+ 52\{321^{12}\}$ $+ 13\{31^{14}\}$ $+ 55\{2^8 1\}$ $+ 81\{2^7 1^3\}$
$+ 72\{2^6 1^5\}$ $+ 56\{2^5 1^7\}$ $+ 40\{2^4 1^9\}$ $+ 24\{2^3 1^{11}\}$ $+ 11\{2^2 1^{13}\}$
$+ 4\{21^{15}\}$ $+ \{1^{17}\}$

sum = 1626621

n = 18

82{18 } + 128{17 1} + 332{16 2} + 226{16 1²} + 526{15 3}
+ 829{15 21} + 387{15 1³} + 768{14 4} + 1683{14 31} + 1148{14 2²}
+ 1464{14 21²} + 484{14 1⁴} + 866{13 5} + 2578{13 41} + 2947{13 32}
+ 3273{13 31²} + 2677{13 2²1} + 2042{13 21³} + 527{13 1⁵} + 902{12 6}
+ 3095{12 51} + 4985{12 42} + 5027{12 41²} + 2517{12 3²} + 7718{12 321}
+ 4638{12 31³} + 2515{12 2³} + 4121{12 2²1²} + 2360{12 21⁴} + 526{12 1⁶}
+ 752{11 7} + 3111{11 61} + 6116{11 52} + 6074{11 51²} + 5548{11 43}
+ 13068{11 421} + 7171{11 41³} + 7532{11 3²1} + 7617{11 32²} + 12268{11 321²}
+ 5373{11 31⁴} + 5056{11 2³1} + 5065{11 2²1³} + 2393{11 21⁵} + 490{11 1⁷}
+ 530{10 8} + 2511{10 71} + 6016{10 62} + 5770{10 61²} + 7348{10 53}
+ 15888{10 521} + 8369{10 51³} + 3576{10 4²} + 16248{10 431} + 13228{10 42²}
+ 20468{10 421²} + 8246{10 41⁴} + 9419{10 3²2} + 12482{10 3²1²} + 16052{10 32²1}
+ 14884{10 321³} + 5446{10 31⁵} + 3499{10 2⁴} + 6756{10 2³1²} + 5258{10 2²1⁴}
+ 2209{10 21⁶} + 428{10 1⁸} + 172{9²} + 1412{981} + 4347{972}
+ 4199{971²} + 6996{963} + 14418{9621} + 7399{961³} + 5759{954}
+ 20723{9531} + 15453{952²} + 23759{9521²} + 9098{951⁴} + 10389{94²1}
+ 20550{9432} + 26131{9431²} + 26944{942²1} + 24122{9421³} + 8058{941⁵}
+ 5020{93³} + 20495{93²21} + 15086{93²1³} + 10951{932³} + 21306{932²1²}
+ 15087{9321⁴} + 4913{931⁶} + 6027{92⁴1} + 7272{92³1³} + 4796{92²1⁵}
+ 1875{921⁷} + 350{91⁹} + 1628{8²2} + 1508{8²1²} + 4252{873}
+ 8594{8721} + 4364{871³} + 5361{864} + 17366{8631} + 12602{862²}
+ 19033{8621²} + 7165{861⁴} + 2455{85²} + 15824{8541} + 24509{8532}
+ 30691{8531²} + 29292{852²1} + 25746{8521³} + 8232{851⁵} + 13698{84²2}
+ 16033{84²1²} + 11149{843²} + 42172{84321} + 29964{8431³} + 17701{842³}
+ 33765{842²1²} + 23115{8421⁴} + 6836{841⁶} + 11519{83³1} + 14534{83²2²}
+ 26775{83²21²} + 14788{83²1⁴} + 18742{832³1} + 21848{832²1³} + 13196{8321⁵}
+ 3955{831⁷} + 3232{82⁵} + 6934{82⁴1²} + 6588{82³1⁴} + 3909{82²1⁶}
+ 1456{821⁸} + 266{81¹⁰ } + 2132{7²4} + 6814{7²31} + 4790{7²2²}
+ 7324{7²21²} + 2698{7²1⁴} + 2348{765} + 11692{7641} + 16732{7632}
+ 20719{7631²} + 19184{762²1} + 16688{7621³} + 5236{761⁵} + 6092{75²1}
+ 18293{7542} + 21324{7541²} + 12177{753²} + 44006{75321} + 30656{7531³}
+ 16861{752³} + 32244{752²1²} + 21570{7521⁴} + 6151{751⁶} + 8772{74²3}
+ 25896{74²21} + 16956{74²1³} + 23553{743²1} + 27714{7432²} + 50043{74321²}
+ 26661{7431⁴} + 27528{742³1} + 31599{742²1³} + 18331{7421⁵} + 5002{741⁷}
+ 9933{73³2} + 14763{73³1²} + 23932{73²2²1} + 25848{73²21³} + 12071{73²1⁵}
+ 9265{732⁴} + 20234{732³1²} + 18334{732²1⁴} + 9937{7321⁶} + 2813{731⁸}
+ 4646{72⁵1} + 6295{72⁴1³} + 5099{72³1⁵} + 2825{72²1⁷} + 1018{721⁹}
+ 185{71¹¹ } + 399{6³} + 3483{6²51} + 8523{6²42} + 9735{6²41²}
+ 5246{6²3²} + 18849{6²321} + 13048{6²31³} + 7059{6²2³} + 13289{6²2²1²}
+ 8872{6²21⁴} + 2467{6²1⁶} + 5696{65²2} + 6480{65²1²} + 9552{6543}
+ 27180{65421} + 17462{6541³} + 20115{653²1} + 22912{6532²} + 41137{65321²}
+ 21498{6531⁴} + 20914{652³1} + 23838{652²1³} + 13576{6521⁵} + 3558{651⁷}
+ 2431{64³} + 16030{64²31} + 15223{64²2²} + 26449{64²21²} + 12952{64²1⁴}
+ 17533{643²2} + 25820{643²1²} + 38826{6432²1} + 41209{64321³} + 18457{6431⁵}
+ 11822{642⁴} + 25424{642³1²} + 22696{642²1⁴} + 11759{6421⁶} + 3033{641⁸}
+ 3041{63⁴} + 15332{63³21} + 13132{63³1³} + 10941{63²2³} + 23390{63²2²1²}
+ 19351{63²21⁴} + 8055{63²1⁶} + 12184{632⁴1} + 16194{632³1³} + 12565{632²1⁵}
+ 6294{6321⁷} + 1723{631⁹} + 1899{62⁶} + 4296{62⁵1²} + 4588{62⁴1⁴}
+ 3340{62³1⁶} + 1769{62²1⁸} + 628{621¹⁰ } + 116{61¹² } + 1951{5³3}
+ 5080{5³21} + 3149{5³1³} + 1616{5²4²} + 10320{5²431} + 9425{5²42²}

n = 18 (Contd)

$+ 16490\{5^2421^2\}$ $+ 7875\{5^241^4\}$ $+ 9135\{5^23^22\}$ $+ 13229\{5^23^21^2\}$ $+ 19474\{5^232^21\}$

$+ 20508\{5^2321^3\}$ $+ 9044\{5^231^5\}$ $+ 5451\{5^22^4\}$ $+ 11878\{5^22^31^2\}$ $+ 10444\{5^22^21^4\}$

$+ 5352\{5^221^6\}$ $+ 1319\{5^21^8\}$ $+ 3454\{54^31\}$ $+ 9441\{54^232\}$ $+ 13422\{54^231^2\}$

$+ 16279\{54^22^21\}$ $+ 16643\{54^221^3\}$ $+ 6793\{54^21^5\}$ $+ 4209\{543^3\}$ $+ 20586\{543^221\}$

$+ 17275\{543^21^3\}$ $+ 13638\{5432^3\}$ $+ 28747\{5432^21^2\}$ $+ 23348\{54321^4\}$ $+ 9304\{5431^6\}$

$+ 11850\{542^41\}$ $+ 15608\{542^31^3\}$ $+ 11837\{542^21^5\}$ $+ 5685\{5421^7\}$ $+ 1417\{541^9\}$

$+ 4376\{53^41\}$ $+ 6500\{53^32^2\}$ $+ 12860\{53^321^2\}$ $+ 8295\{53^31^4\}$ $+ 12191\{53^22^31\}$

$+ 15592\{53^22^21^3\}$ $+ 10955\{53^221^5\}$ $+ 4195\{53^21^7\}$ $+ 4031\{532^5\}$ $+ 9394\{532^41^2\}$

$+ 9699\{532^31^4\}$ $+ 6752\{532^21^6\}$ $+ 3218\{5321^8\}$ $+ 876\{531^{10}\}$ $+ 2037\{52^61\}$

$+ 2922\{52^51^3\}$ $+ 2638\{52^41^5\}$ $+ 1797\{52^31^7\}$ $+ 933\{52^21^9\}$ $+ 336\{521^{11}\}$

$+ 65\{51^{13}\}$ $+ 1311\{4^42\}$ $+ 1666\{4^41^2\}$ $+ 1388\{4^33^2\}$ $+ 6350\{4^3321\}$

$+ 5138\{4^331^3\}$ $+ 3403\{4^32^3\}$ $+ 6913\{4^32^21^2\}$ $+ 5424\{4^321^4\}$ $+ 1960\{4^31^6\}$

$+ 3463\{4^23^31\}$ $+ 4940\{4^23^22^2\}$ $+ 9805\{4^23^221^2\}$ $+ 6155\{4^23^21^4\}$ $+ 8666\{4^232^31\}$

$+ 10964\{4^232^21^3\}$ $+ 7538\{4^2321^5\}$ $+ 2781\{4^231^7\}$ $+ 2346\{4^22^5\}$ $+ 5303\{4^22^41^2\}$

$+ 5471\{4^22^31^4\}$ $+ 3698\{4^22^21^6\}$ $+ 1706\{4^221^8\}$ $+ 427\{4^21^{10}\}$ $+ 1808\{43^42\}$

$+ 2874\{43^41^2\}$ $+ 5456\{43^32^21\}$ $+ 6420\{43^321^3\}$ $+ 3460\{43^31^5\}$ $+ 3010\{43^22^4\}$

$+ 6946\{43^22^31^2\}$ $+ 6824\{43^22^21^4\}$ $+ 4293\{43^221^6\}$ $+ 1568\{43^21^8\}$ $+ 3268\{432^51\}$

$+ 4613\{432^41^3\}$ $+ 4066\{432^31^5\}$ $+ 2632\{432^21^7\}$ $+ 1240\{4321^9\}$ $+ 348\{431^{11}\}$

$+ 564\{42^7\}$ $+ 1266\{42^61^2\}$ $+ 1422\{42^51^4\}$ $+ 1146\{42^41^6\}$ $+ 760\{42^31^8\}$

$+ 400\{42^21^{10}\}$ $+ 151\{421^{12}\}$ $+ 32\{41^{14}\}$ $+ 149\{3^6\}$ $+ 876\{3^521\}$

$+ 813\{3^51^3\}$ $+ 791\{3^42^3\}$ $+ 1711\{3^42^21^2\}$ $+ 1550\{3^421^4\}$ $+ 746\{3^41^6\}$

$+ 1343\{3^32^41\}$ $+ 1859\{3^32^31^3\}$ $+ 1558\{3^32^21^5\}$ $+ 918\{3^321^7\}$ $+ 336\{3^31^9\}$

$+ 458\{3^22^6\}$ $+ 1124\{3^22^51^2\}$ $+ 1207\{3^22^41^4\}$ $+ 964\{3^22^31^6\}$ $+ 608\{3^22^21^8\}$

$+ 296\{3^221^{10}\}$ $+ 89\{3^21^{12}\}$ $+ 334\{32^71\}$ $+ 483\{32^61^3\}$ $+ 450\{32^51^5\}$

$+ 344\{32^41^7\}$ $+ 232\{32^31^9\}$ $+ 128\{32^21^{11}\}$ $+ 52\{321^{13}\}$ $+ 13\{31^{15}\}$

$+ 43\{2^9\}$ $+ 74\{2^81^2\}$ $+ 88\{2^71^4\}$ $+ 72\{2^61^6\}$ $+ 56\{2^51^8\}$

$+ 40\{2^41^{10}\}$ $+ 24\{2^31^{12}\}$ $+ 11\{2^21^{14}\}$ $+ 4\{21^{16}\}$ $+ \{1^{18}\}$

sum = 3468080

n = 19

91{19 } + 145{18 1} + 377{17 2} + 257{17 1^2} + 610{16 3}
+ 956{16 21} + 444{16 1^3} + 901{15 4} + 1972{15 31} + 1339{15 2^2}
+ 1710{15 21^2} + 563{15 1^4} + 1051{14 5} + 3090{14 41} + 3516{14 32}
+ 3891{14 31^2} + 3178{14 2^{2}1} + 2418{14 21^3} + 623{14 1^5} + 1125{13 6}
+ 3826{13 51} + 6097{13 42} + 6149{13 41^2} + 3070{13 3^2} + 9376{13 321}
+ 5623{13 31^3} + 3036{13 2^3} + 4982{13 2^{2}1^2} + 2846{13 21^4} + 633{13 1^6}
+ 1012{12 7} + 4042{12 61} + 7804{12 52} + 7713{12 51^2} + 6996{12 43}
+ 16411{12 421} + 8980{12 41^3} + 9394{12 3^{2}1} + 9489{12 32^2} + 15250{12 321^2}
+ 6672{12 31^4} + 6257{12 2^{3}1} + 6260{12 2^{2}1^3} + 2956{12 21^5} + 603{12 1^7}
+ 785{11 8} + 3546{11 71} + 8163{11 62} + 7836{11 61^2} + 9759{11 53}
+ 20999{11 521} + 11031{11 51^3} + 4682{11 4^2} + 21168{11 431} + 17155{11 42^2}
+ 26543{11 421^2} + 10660{11 41^4} + 12135{11 3^{2}2} + 16050{11 3^{2}1^2} + 20584{11 32^{2}1}
+ 19069{11 321^3} + 6968{11 31^5} + 4450{11 2^4} + 8609{11 2^{3}1^2} + 6693{11 2^{2}1^4}
+ 2813{11 21^6} + 543{11 1^8} + 421{10 9} + 2456{10 81} + 6740{10 72}
+ 6443{10 71^2} + 10190{10 63} + 20854{10 621} + 10654{10 61^3} + 8140{10 54}
+ 28922{10 531} + 21512{10 52^2} + 32963{10 521^2} + 12601{10 51^4} + 14276{10 4^{2}1}
+ 27990{10 432} + 35525{10 431^2} + 36505{10 42^{2}1} + 32634{10 421^3} + 10887{10 41^5}
+ 6727{10 3^3} + 27457{10 3^{2}21} + 20199{10 3^{2}1^3} + 14624{10 32^3} + 28407{10 32^{2}1^2}
+ 20123{10 321^4} + 6546{10 31^6} + 7976{10 2^{4}1} + 9619{10 2^{3}1^3} + 6353{10 2^{2}1^5}
+ 2483{10 21^7} + 462{10 1^9} + 864{9^{2}1} + 3841{982} + 3627{981^2}
+ 7669{973} + 15378{9721} + 7775{971^3} + 8678{964} + 27816{9631}
+ 20001{962^2} + 30229{9621^2} + 11310{961^4} + 3835{95^2} + 24072{9541}
+ 36832{9532} + 46024{9531^2} + 43685{952^{2}1} + 38332{9521^3} + 12224{951^5}
+ 20043{94^{2}2} + 23469{94^{2}1^2} + 16188{943^2} + 60982{94321} + 43263{9431^3}
+ 25428{942^3} + 48544{942^{2}1^2} + 33197{9421^4} + 9819{941^6} + 16327{93^{3}1}
+ 20581{93^{2}2^2} + 37870{93^{2}21^2} + 20926{93^{2}1^4} + 26382{932^{3}1} + 30763{932^{2}1^3}
+ 18604{9321^5} + 5579{931^7} + 4487{92^5} + 9661{92^{4}1^2} + 9181{92^{3}1^4}
+ 5466{92^{2}1^6} + 2034{921^8} + 369{91^{10} } + 2883{8^{2}3} + 5671{8^{2}21}
+ 2829{8^{2}1^3} + 5540{874} + 17092{8731} + 12027{872^2} + 18144{8721^2}
+ 6689{871^4} + 4700{865} + 22486{8641} + 31578{8632} + 38955{8631^2}
+ 35798{862^{2}1} + 31048{8621^3} + 9707{861^5} + 10774{85^{2}1} + 31343{8542}
+ 36371{8541^2} + 20471{853^2} + 73794{85321} + 51325{8531^3} + 28075{852^3}
+ 53515{852^{2}1^2} + 35808{8521^4} + 10176{851^6} + 14177{84^{2}3} + 41654{84^{2}21}
+ 27216{84^{2}1^3} + 37295{843^{2}1} + 43791{8432^2} + 79015{84321^2} + 42104{8431^4}
+ 43135{842^{3}1} + 49519{842^{2}1^3} + 28773{8421^5} + 7846{841^7} + 15201{83^{3}2}
+ 22641{83^{3}1^2} + 36592{83^{2}2^{2}1} + 39565{83^{2}21^3} + 18509{83^{2}1^5} + 14085{832^4}
+ 30722{832^{3}1^2} + 27921{832^{2}1^4} + 15175{8321^6} + 4301{831^8} + 6943{82^{5}1}
+ 9418{82^{4}1^3} + 7664{82^{3}1^5} + 4260{82^{2}1^7} + 1533{821^9} + 274{81^{11} }
+ 2052{7^{2}5} + 9162{7^{2}41} + 12428{7^{2}32} + 15325{7^{2}31^2} + 13817{7^{2}2^{2}1}
+ 11946{7^{2}21^3} + 3683{7^{2}1^5} + 1267{76^2} + 10290{7651} + 23589{7642}
+ 27040{7641^2} + 14322{763^2} + 50700{76321} + 34919{7631^3} + 18606{762^3}
+ 35248{762^{2}1^2} + 23386{7621^4} + 6505{761^6} + 12633{75^{2}2} + 14275{75^{2}1^2}
+ 20072{7543} + 56668{75421} + 36301{7541^3} + 40937{753^{2}1} + 46375{7532^2}
+ 83178{75321^2} + 43414{7531^4} + 41737{752^{3}1} + 47575{752^{2}1^3} + 27105{7521^5}
+ 7092{751^7} + 4580{74^3} + 30021{74^{2}31} + 28290{74^{2}2^2} + 49282{74^{2}21^2}
+ 24081{74^{2}1^4} + 31899{743^{2}2} + 46907{743^{2}1^2} + 70288{7432^{2}1} + 74684{74321^3}
+ 33524{7431^5} + 21086{742^4} + 45520{742^{3}1^2} + 40693{742^{2}1^4} + 21175{7421^6}
+ 5444{741^8} + 5222{73^4} + 26394{73^{3}21} + 22654{73^{3}1^3} + 18786{73^{2}2^3}
+ 40163{73^{2}2^{2}1^2} + 33371{73^{2}21^4} + 13943{73^{2}1^6} + 20662{732^{4}1} + 27549{732^{3}1^3}
+ 21489{732^{2}1^5} + 10812{7321^7} + 2948{731^9} + 3111{72^6} + 7112{72^{5}1^2}

n = 19 (Contd)

$+ 7622\{72^41^4\}$ $+ 5596\{72^31^6\}$ $+ 2965\{72^21^8\}$ $+ 1045\{721^{10}\}$ $+ 187\{71^{12}\}$

$+ 1672\{6^31\}$ $+ 7387\{6^252\}$ $+ 8199\{6^251^2\}$ $+ 9489\{6^243\}$ $+ 26340\{6^2421\}$

$+ 16715\{6^241^3\}$ $+ 17873\{6^23^21\}$ $+ 20049\{6^232^2\}$ $+ 35747\{6^2321^2\}$ $+ 18537\{6^231^4\}$

$+ 17394\{6^22^31\}$ $+ 19738\{6^22^21^3\}$ $+ 11163\{6^221^5\}$ $+ 2861\{6^21^7\}$ $+ 6927\{65^23\}$

$+ 17947\{65^221\}$ $+ 11067\{65^21^3\}$ $+ 5391\{654^2\}$ $+ 32949\{65431\}$ $+ 29945\{6542^2\}$

$+ 52031\{65421^2\}$ $+ 24858\{6541^4\}$ $+ 27615\{653^22\}$ $+ 40205\{653^21^2\}$ $+ 58472\{6532^21\}$

$+ 61622\{65321^3\}$ $+ 27134\{6531^5\}$ $+ 16085\{652^4\}$ $+ 34794\{652^31^2\}$ $+ 30785\{652^21^4\}$

$+ 15729\{6521^6\}$ $+ 3872\{651^8\}$ $+ 8524\{64^31\}$ $+ 22753\{64^232\}$ $+ 32310\{64^231^2\}$

$+ 38866\{64^22^21\}$ $+ 39772\{64^221^3\}$ $+ 16248\{64^21^5\}$ $+ 9634\{643^3\}$ $+ 47154\{643^221\}$

$+ 39674\{643^21^3\}$ $+ 30984\{6432^3\}$ $+ 65397\{6432^21^2\}$ $+ 53336\{64321^4\}$ $+ 21304\{6431^6\}$

$+ 26341\{642^41\}$ $+ 34818\{642^31^3\}$ $+ 26569\{642^21^5\}$ $+ 12782\{6421^7\}$ $+ 3157\{641^9\}$

$+ 9041\{63^41\}$ $+ 13368\{63^32^2\}$ $+ 26599\{63^321^2\}$ $+ 17216\{63^31^4\}$ $+ 24963\{63^22^31\}$

$+ 32085\{63^22^21^3\}$ $+ 22692\{63^221^5\}$ $+ 8721\{63^21^7\}$ $+ 8079\{632^5\}$ $+ 18824\{632^41^2\}$

$+ 19620\{632^31^4\}$ $+ 13744\{632^21^6\}$ $+ 6557\{6321^8\}$ $+ 1752\{631^{10}\}$ $+ 3872\{62^61\}$

$+ 5595\{62^51^3\}$ $+ 5113\{62^41^5\}$ $+ 3501\{62^31^7\}$ $+ 1803\{62^21^9\}$ $+ 633\{621^{11}\}$

$+ 116\{61^{13}\}$ $+ 1387\{5^34\}$ $+ 6735\{5^331\}$ $+ 5667\{5^32^2\}$ $+ 9774\{5^321^2\}$

$+ 4468\{5^31^4\}$ $+ 5897\{5^24^21\}$ $+ 14733\{5^2432\}$ $+ 20775\{5^2431^2\}$ $+ 24356\{5^242^21\}$

$+ 24726\{5^2421^3\}$ $+ 9927\{5^241^5\}$ $+ 5105\{5^23^3\}$ $+ 24484\{5^23^221\}$ $+ 20403\{5^23^21^3\}$

$+ 15582\{5^232^3\}$ $+ 32857\{5^232^21^2\}$ $+ 26530\{5^2321^4\}$ $+ 10429\{5^231^6\}$ $+ 12306\{5^22^41\}$

$+ 16214\{5^22^31^3\}$ $+ 12255\{5^22^21^5\}$ $+ 5787\{5^221^7\}$ $+ 1374\{5^21^9\}$ $+ 5405\{54^32\}$

$+ 7065\{54^31^2\}$ $+ 5670\{54^23^2\}$ $+ 25570\{54^2321\}$ $+ 20656\{54^231^3\}$ $+ 13314\{54^22^3\}$

$+ 27474\{54^22^21^2\}$ $+ 21480\{54^221^4\}$ $+ 7785\{54^21^6\}$ $+ 12657\{543^31\}$ $+ 18103\{543^22^2\}$

$+ 35740\{543^221^2\}$ $+ 22593\{543^21^4\}$ $+ 31052\{5432^31\}$ $+ 39446\{5432^21^3\}$ $+ 27256\{543321^5\}$

$+ 10027\{5431^7\}$ $+ 7929\{542^5\}$ $+ 18295\{542^41^2\}$ $+ 18877\{542^31^4\}$ $+ 12894\{542^21^6\}$

$+ 5881\{5421^8\}$ $+ 1433\{541^{10}\}$ $+ 5047\{53^42\}$ $+ 8064\{53^41^2\}$ $+ 15193\{53^32^21\}$

$+ 17952\{53^321^3\}$ $+ 9727\{53^31^5\}$ $+ 8231\{53^22^4\}$ $+ 18998\{53^22^31^2\}$ $+ 18844\{53^22^21^4\}$

$+ 11911\{53^221^6\}$ $+ 4328\{53^21^8\}$ $+ 8500\{532^51\}$ $+ 12125\{532^41^3\}$ $+ 10796\{532^31^5\}$

$+ 7011\{532^21^7\}$ $+ 3256\{5321^9\}$ $+ 877\{531^{11}\}$ $+ 1284\{52^7\}$ $+ 2990\{52^61^2\}$

$+ 3384\{52^51^4\}$ $+ 2775\{52^41^6\}$ $+ 1823\{52^31^8\}$ $+ 936\{52^21^{10}\}$ $+ 336\{521^{12}\}$

$+ 65\{51^{14}\}$ $+ 1003\{4^43\}$ $+ 3520\{4^421\}$ $+ 2615\{4^41^3\}$ $+ 4270\{4^33^21\}$

$+ 5705\{4^332^2\}$ $+ 11027\{4^3321^2\}$ $+ 6669\{4^331^4\}$ $+ 7655\{4^32^31\}$ $+ 9507\{4^32^21^3\}$

$+ 6264\{4^321^5\}$ $+ 2103\{4^31^7\}$ $+ 3998\{4^23^32\}$ $+ 6369\{4^23^31^2\}$ $+ 11661\{4^23^22^21\}$

$+ 13596\{4^23^221^3\}$ $+ 7202\{4^23^21^5\}$ $+ 5907\{4^232^4\}$ $+ 13456\{4^232^31^2\}$ $+ 13211\{4^232^21^4\}$

$+ 8144\{4^2321^6\}$ $+ 2855\{4^231^8\}$ $+ 4849\{4^22^51\}$ $+ 6877\{4^22^41^3\}$ $+ 6033\{4^22^31^5\}$

$+ 3833\{4^22^21^7\}$ $+ 1712\{4^221^9\}$ $+ 427\{4^21^{11}\}$ $+ 781\{43^5\}$ $+ 4478\{43^421\}$

$+ 4151\{43^41^3\}$ $+ 3896\{43^32^3\}$ $+ 8632\{43^32^21^2\}$ $+ 7781\{43^321^4\}$ $+ 3748\{43^31^6\}$

$+ 6424\{43^22^41\}$ $+ 8949\{43^22^31^3\}$ $+ 7553\{43^22^21^5\}$ $+ 4422\{43^221^7\}$ $+ 1575\{43^21^9\}$

$+ 2013\{432^6\}$ $+ 4816\{432^51^2\}$ $+ 5324\{432^41^4\}$ $+ 4246\{432^31^6\}$ $+ 2653\{432^21^8\}$

$+ 1240\{4321^{10}\}$ $+ 348\{431^{12}\}$ $+ 1085\{42^71\}$ $+ 1592\{42^61^3\}$ $+ 1513\{42^51^5\}$

$+ 1163\{42^41^7\}$ $+ 760\{42^31^9\}$ $+ 400\{42^21^{11}\}$ $+ 151\{421^{13}\}$ $+ 32\{41^{15}\}$

$+ 426\{3^61\}$ $+ 701\{3^52^2\}$ $+ 1431\{3^521^2\}$ $+ 1006\{3^51^4\}$ $+ 1672\{3^42^31\}$

$+ 2241\{3^42^21^3\}$ $+ 1706\{3^421^5\}$ $+ 768\{3^41^7\}$ $+ 832\{3^32^5\}$ $+ 1994\{3^32^41^2\}$

$+ 2131\{3^32^31^4\}$ $+ 1624\{3^32^21^6\}$ $+ 920\{3^321^8\}$ $+ 336\{3^31^{10}\}$ $+ 953\{3^22^61\}$

$+ 1377\{3^22^51^3\}$ $+ 1296\{3^22^41^5\}$ $+ 968\{3^22^31^7\}$ $+ 608\{3^22^21^9\}$ $+ 296\{3^221^{11}\}$

$+ 89\{3^21^{13}\}$ $+ 210\{32^8\}$ $+ 473\{32^71^2\}$ $+ 536\{32^61^4\}$ $+ 456\{32^51^6\}$

$+ 344\{32^41^8\}$ $+ 232\{32^31^{10}\}$ $+ 128\{32^21^{12}\}$ $+ 52\{321^{14}\}$ $+ 13\{31^{16}\}$

$+ 64\{2^91\}$ $+ 96\{2^81^3\}$ $+ 88\{2^71^5\}$ $+ 72\{2^61^7\}$ $+ 56\{2^51^9\}$

$+ 40\{2^41^{11}\}$ $+ 24\{2^31^{13}\}$ $+ 11\{2^21^{15}\}$ $+ 4\{21^{17}\}$ $+ \{1^{19}\}$

sum = 7236303